

The background of the book cover is a composite image. It features an aerial photograph of a city, likely San Francisco, with visible landmarks like the Golden Gate Bridge and the city grid. Overlaid on this is a semi-transparent image of a green printed circuit board (PCB) with intricate blue and white circuit traces. The title 'Advanced Control Engineering' is prominently displayed in the upper half of the cover.

Advanced Control Engineering

Roland S. Burns



Advanced Control Engineering

In fond memory of
my mother

Advanced Control Engineering

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